

## An Adversarial Network-based Multi-model Black-box Attack

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**Abstract:** Researches have shown that Deep neural networks (DNNs) are vulnerable to adversarial examples. In this paper, we propose a generative model to explore how to produce adversarial examples that can deceive multiple deep learning models simultaneously. Unlike most of popular adversarial attack algorithms, the one proposed in this paper is based on the Generative Adversarial Networks (GAN). It can quickly produce adversarial examples and perform black-box attacks on multi-model. To enhance the transferability of the samples generated by our approach, we use multiple neural networks in the training process. Experimental results on MNIST showed that our method can efficiently generate adversarial examples. Moreover, it can successfully attack various classes of deep neural networks at the same time, such as fully connected neural networks (FCNN), convolutional neural networks (CNN) and recurrent neural networks (RNN). We performed a black-box attack on VGG16 and the experimental results showed that when the test data classes are ten (0–9), the attack success rate is 97.68%, and when the test data classes are seven (0–6), the attack success rate is up to 98.25%.

**Keywords:** Black-box attack; adversarial examples; GAN; multi-model; deep neural networks

### 1 Introduction

Deep neural networks have achieved great success in various computer vision tasks, such as image recognition [1,2], object detection [3] and semantic segmentation [4], etc. However, recent research has shown that deep neural networks are vulnerable to adversarial examples [5], a modification of the clean image by adding well-designed perturbations in a way that the changes are imperceptible to the human eye. Since adversarial examples were introduced, adversarial attacks have attracted a lot of attention [6,7]. Most of current attack algorithms are gradient-based white-box attacks [8] which have the complete knowledge of the targeted model including its parameter values, architecture and calculate the gradient of the model to generate the adversarial examples with neural networks, but these adversarial examples have



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poor transferability and can attack specific deep learning models only. In fact, it is undeniable that in some instances, the adversary has a limited knowledge of the model, which in turn leads to unsuccessful attacks. Therefore, it is of great importance to study black-box attacks which can make up for the deficiency of the white box attacks.

Fig. 1 shows clean images in the front row and their corresponding adversarial images in the bottom row. These adversarial images are still recognizable to the human eye, but can fool the deep learning models. Since white-box attacks have their deficiency mentioned above, to address this issue, we propose a black-box attack algorithm to produce adversarial examples that can fool DNNs even with limited knowledge of the model by using multiple classification (MC) models and distilling useful models to train the generator and discriminator.



Figure 1: Comparison of clean images and adversarial images

## 2 Related Work

### 2.1 Adversarial Examples

Adversarial examples were introduced in 2013 by Szegedy et al. and their researches have demonstrated that deep neural networks, CNNs included are vulnerable to adversarial examples. Meanwhile, there are many other researches dedicated to adversarial attacks. The majority of them are based on optimization by minimizing the distance between the adversarial images and the clean images so as to cause the model to make wrong classification prediction. Some attack strategies require access to the gradients or parameters of the model, yet these strategies are limited to gradient-based models only. (e.g., neural networks). Others only need have access to the output of the model.

Fig. 2 is the generation process of adversarial examples. The attack algorithm firstly computes the perturbations by calling the deep learning model and then creates the adversarial examples by adding the perturbations to the clean images to fool the model.

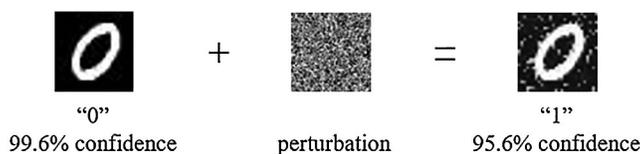


Figure 2: Generating adversarial example

### 2.2 Attack Methods

There are two common types of adversarial attacks: white-box attacks and black-box attacks. The adversarial attacks are called white-box attacks when the complete information of the targeted model is fully known to the adversary. Alternatively, when the adversary has limited knowledge of the targeted model and creates adversarial examples by having access to the input and output of the model, they are called black-box attacks. Among the existing attacks, the white-box attack algorithm predominates.

### 2.2.1 White-box Attacks

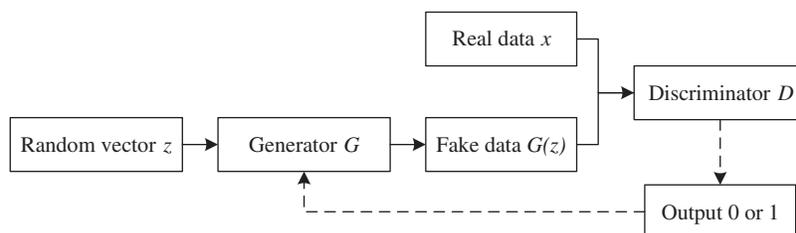
In white-box attacks, L-BFGS [9] is one of white-box attacks to generate adversarial examples for deep learning model. However, there are imperfections in this attack algorithm. For example, it is very slow to generate the adversarial examples and these examples can be well-defended by reducing their quality. Goodfellow et al. [10] proposed Fast Gradient Sign Method (FGSM), which generates adversarial examples by incrementing the gradient direction of the model loss. Due to the high computational cost of L-BFGS and the low attack success rate of FGSM, the Basic Iterative Method, also called I-FGSM, was proposed by Kurakin et al. [11]. BIM can reduce the computational costs with iterative optimization and increase the attack success rate, so highly-aggressive adversarial examples can be created after a small number of iterations. Projected Gradient Descend (PGD) in Madry et al. [12] which can produce adversarial examples via randomly initializing the search in a certain azimuth class of the clean images and then iterating several times and as a result, it became the most powerful first-order adversarial attack. That is, if the defense method can successfully defend the attack of PGD algorithm, then it can defend other first-order attack algorithms as well. Carlini et al. [13] attack (C&W) designed a loss function and a search for adversarial examples by minimizing the loss function and they applied Adam [14], which projects the results onto box constraints at each step to achieve the strongest L2 attack, so as to solve the optimization problem and handled box constraints.

### 2.2.2 Black-box Attacks

Black-box attacks have two categories: those with probing and those without probing. As for the former, the adversary knows little or nothing about the model but can have access to the model's output through the input, while the latter implies that the adversary has limited knowledge of the model. Some studies [15,16] pointed out that adversarial examples generated by black-box attacks can fool more than one model.

## 2.3 Generative Adversarial Networks

The generative adversarial networks proposed by Goodfellow et al. [17] is an unsupervised learning algorithm inspired by the two-person zero-sum games in game theory. Its unique adversarial training idea can generate high quality examples, so it has more powerful feature learning and representation capabilities than traditional machine learning algorithms. GAN consists of a generator and a discriminator, each of which updates its own parameters to minimize the loss during the training process of the model, and finally reaches a Nash equilibrium state through continuous iterative optimization. However, there is no way to control the model because the process is too free in generating larger images. To overcome the limitations of GAN, Conditional GAN (CGAN) was proposed by Mirza et al. [18] and they added constraints to the original GAN to direct the sample generation process. After that, many advancements in designing and training GAN models have been made, most significantly the Deep Convolutional GAN (DCGAN) proposed by Radford et al. [19], which is a combination of CNN and GAN and has substantially improved the quality and diversity of the generated images. Fig. 3 is a schematic diagram of the structure of GAN.



**Figure 3:** Generative adversarial networks [17]

### 3 Methodology

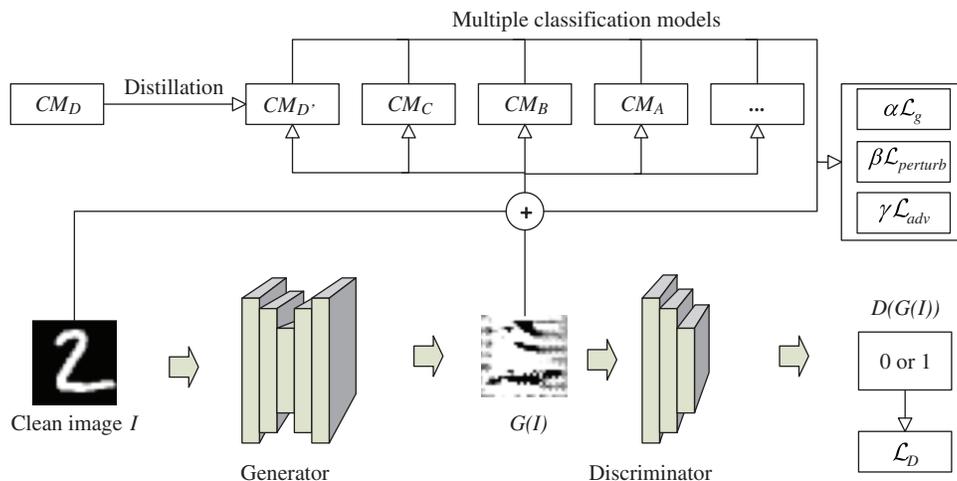
#### 3.1 Problem Definition

Suppose  $I$  is a clean image,  $I_a$  is an adversarial image,  $G$  is a generator,  $D$  is a discriminator, and  $CM_A$ ,  $CM_B$ ,  $CM_C$ ,  $CM_D$  are four classification models, where  $CM_A$  is a CNN,  $CM_B$  is a FCNN,  $CM_C$  is a RNN, and  $CM_D$  is a CNN with a more complex structure. We choose  $CM_A$  as a local model and distill model [20]  $CM_{D'}$  from  $CM_D$ . We expect to train the generator and discriminator by calling  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_{D'}$ . As a result, the adversarial examples generated by this trained model are able to attack  $CM_D$  with a high attack success rate (ASR).  $I$  and  $I_a$  can be expressed by the following equation:

$$I_a = I + G(I) \quad (1)$$

#### 3.2 Network Architecture

The model proposed in the paper consists of a generator and a discriminator of GAN. The generator is similar to the way the encoding network in VAE [21], where examples are input to generate perturbations, and then these perturbations are added to the original input to get the adversarial examples. While the discriminator is a simply a classifier and it is used to distinguish the clean images from the adversarial images created by the generator. The model is shown in Fig. 4.



**Figure 4:** Structure of our method. The clean image  $I$  is passed into the generator to obtain  $G(I)$ .  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_D$  are four classification models which are FCNN, CNN, LSTM and VGG16 [22].  $CM_{D'}$  is the distillation model of  $CM_D$ .  $G(I)$  is input into the four classification models in the figure, and the output of the model (probability) and the generator loss can be obtained. Then  $G(I)$  is input into the discriminator and discriminator loss can be calculated

Tab. 1 is the structure of the generator.

The network architecture of discriminator is similar to that in DCGAN. The clean and generated images are respectively fed into the discriminator and then passes three convolutional layers, one fully connected layer and a sigmoid activation function. The discriminator  $D$  is to make the prediction of the clean images as close to 1 as possible and the generated images approximate 0. The network architecture of discriminator is presented in Tab. 2.

**Table 1:** Generator structure

Layer type	Output dimension	Activation
Convolutional layer	(7,7,32)	ReLU
Residual block	(7,7,32)	ReLU
Deconvolutional layer	(28,28,1)	ReLU

**Table 2:** Discriminator structure

Layer type	Output dimension	Activation
Convolutional layer	(2,2,32)	LeakyReLU
Instance Normalization	128	None
Fully connected layer	1	Sigmoid

### 3.3 The Algorithm for Generating Adversarial Examples

The algorithm for generating adversarial examples is as follows. The inputs are clean image  $I$  and four pre-trained models, the output is the adversarial images. The whole process starts with obtaining the distillation model  $CM_D$  and then the model is trained according to Eqs. (2) and (5) to minimize the loss so that the model output the adversarial images successfully.

**Algorithm 1:** Training generative model to generated adversarial images

**Input:** Clean images  $I$ , pretrained models  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_D$

**Output:** Adversarial images  $I_a$

1.  $G \leftarrow$  Generator ();
2.  $D \leftarrow$  Discriminator ();
3.  $CM_D \leftarrow$  Distill model  $CM_D$ ; //  $CM_A$  as a local model
4. **for** each  $I$  in train set **do**
5.      $x \leftarrow G(I)$ ;
6.      $I_a \leftarrow I + x$ ;
7.      $CM(I_a)$ ; //Get the probability of  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_D$
8.     Minimize the loss of discriminator with Eq. (2);
9.     Minimize the loss of generator with Eq. (5);
10. **end for**
11. **return**  $I_a$ ;

### 3.4 Loss Function

The loss function of the generative model contains that of the discriminator and generator. The loss function of the discriminator can be described as follows:

$$\mathcal{L}_D = \mathcal{L}_{fake} + \mathcal{L}_{real} \quad (2)$$

To make the discriminator converge, we choose the mean square error (MSE) [23] as the loss function of the discriminator. From Eq. (2), it can be seen that the loss function is made up of the real and the fake loss. Where the real loss can be described as:

$$\mathcal{L}_{real} = MSE(D(I), 1) \quad (3)$$

$I$  refers to the clean image, and  $D(I)$  is the output. Since training the discriminator is to make the clean image approach to 1,  $D(I)$  is combined with the all-1 vector to compute the MSE. Meanwhile, we expect the generated image to become near 0, so the generated examples loss can be expressed as follows:

$$\mathcal{L}_{fake} = MSE(D(G(I)) + I, 0) \quad (4)$$

The loss function of the generator consists of three parts, as shown in Eq. (5), on the premise of  $\alpha = \beta = \gamma = 1$ , the generated adversarial examples are best.

$$\mathcal{L}_G = \alpha\mathcal{L}_g + \beta\mathcal{L}_{perturb} + \gamma\mathcal{L}_{adv} \quad (5)$$

The first part is to make the generated image as close to the real image, so the first part is MSE, as shown in Eq. (6).

$$\mathcal{L}_g = MSE(G(I) + I, 1) \quad (6)$$

The goal of the second part is making the output  $G(I)$  of the generator as close as to 0, so we add the hinge loss to the  $L_2$  norm.  $\varepsilon$  is a hyperparameter used to stabilize the training of generator.

$$\mathcal{L}_{perturb} = \max(0, \|G(I)\|_2 - \varepsilon) \quad (7)$$

The third part is to enable the generated examples to deceive the classification model, so the loss function can be defined by:

$$\mathcal{L}_{adv} = f(C(G(I) + I), y) \quad (8)$$

In Eq. (8),  $C$  represents the multiple models, including  $CM_A$ ,  $CM_B$ ,  $CM_C$  and the distillation model  $CM_D$ ,  $f$  stands for the loss function and  $y$  symbolizes the one-hot vector transformed from the real label. As a result, its probability value can be obtained by adding the output of the generator and the clean image as the input of the multiple models, and then the loss can be calculated by using label  $y$ .

## 4 Experiment

### 4.1 Environment and Dataset

For the experimental environment, TensorFlow was applied as the deep learning framework, and the graphics card was NVIDIA GeForce GTX1080Ti. CUDA and cuDNN were configured for graphics card acceleration training.

The data set in the experiment was the MNIST handwritten digits data set, which consists of 60,000 train set images and 10,000 test set images. These images have been pre-processed with a uniform size of 28\*28, which reduces the complex operations of data collection and pre-processing, and allow us to utilize them with only some normalization.

### 4.2 Threat Model

$CM_A$  is used as a local model to get the distillation model  $CM_D$  from  $CM_D$ , and our goal is training the generative model by calling the multi-model (excluding model  $CM_D$ ). The generated adversarial examples can not only attack multi-model for auxiliary training but also the model  $CM_D$ , i.e., VGG16.

### 4.3 Results and Analysis

White-box attacks are the most commonly used in adversarial attacks and they have their deficiency mentioned above. To prove that our method is effective, we generated 10,000 adversarial examples with an assumption of the test data set of MNIST, as shown in Fig. 5, and then classified them with  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_D$  respectively. Tab. 3 shows the black-box attack algorithm proposed by Xiao et al. [24].



**Figure 5:** A comparison of clean images and adversarial images. The first two rows are clean images sampled from the MNIST data set, and the last two rows are their corresponding adversarial images produced by our method, which are able to force  $CM_D$  to make wrong classification prediction with limited knowledge of the model  $CM_D$

**Table 3:** Accuracy (%) on MNIST-10 of different models for pristine data and adversarial examples

Model	$CM_A$	$CM_B$	$CM_C$	$CM_D$
Accuracy (p)	99.27	99.88	98.38	99.98
$CM'$	0.98	33.42	61.27	65.78
ASR (b-S)	Null	48.80	54.32	38.42
ASR (b-D)	Null	98.12	98.54	97.39

p: pristine test data;  $CM'$ : distillation model of classification model; b-S: black-box attack with static distillation strategies; b-D: black-box attack with dynamic distillation strategies; Null:  $CM_A$  as a local model.

$CM_A$  as a local model,  $CM'$  as the distillation model get by  $CM_A$  distilling  $CM_B$ ,  $CM_C$  and  $CM_D$  respectively. They are used as the target models for training the generative models. Accuracy is calculated on models  $CM_A$ ,  $CM_B$ ,  $CM_C$  and  $CM_D$  after obtaining the adversarial examples.

As we can see in Tab. 4, we have adopted multi-model to train the generative model, and the ASR of  $CM_D$  has been improved for both static and dynamic distillation. We also experiment on MNIST with 7 classes (0–6) further improved by ASR, and the experimental results are shown in Tab. 5.

As shown in the table above, the ASR of VGG16 has increased from 97.39% to 98.25%, which proves that our method can effectively perform black-box attack on VGG16.

**Table 4:** ASR (%) on MNIST-10 of different models on adversarial examples

Model	$CM_A \& CM_B \& CM_C$	$CM_A \& CM_B \& CM_C \& CM'$ (b-S)	$CM_A \& CM_B \& CM_C \& CM'$ (b-D)
ASR	$CM_A$ 99.00	99.16	98.94
	$CM_B$ 99.20	99.16	99.26
	$CM_C$ 99.58	99.61	99.31
	$CM_D$ 37.37	<b>45.13</b>	<b>97.67</b>

The first column represents the multi-model in the training of the generator.

**Table 5:** ASR (%) on MNIST-7

Model	$CM_A \& CM_B \& CM_C \& CM'$ (b-S)	$CM_A \& CM_B \& CM_C \& CM'$ (b-D)
ASR	$CM_A$ 99.38	98.27
	$CM_B$ 99.67	99.59
	$CM_C$ 99.79	99.64
	$CM_D$ <b>54.08</b>	<b>98.25</b>

## 5 Conclusion

In this paper, we proposed a black-box attack algorithm based on the GAN network architecture. Compared with other adversarial attack algorithms, this method generates adversarial examples with better transferability and higher ASR for the model. We use various classes of neural networks to assist in the training of the model, and experiments conducted on MNIST have validated the effectiveness and efficiency of our method.

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**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

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